

CSCI 201: Data Structures

Fall 2024

Lecture 4R: Sorting

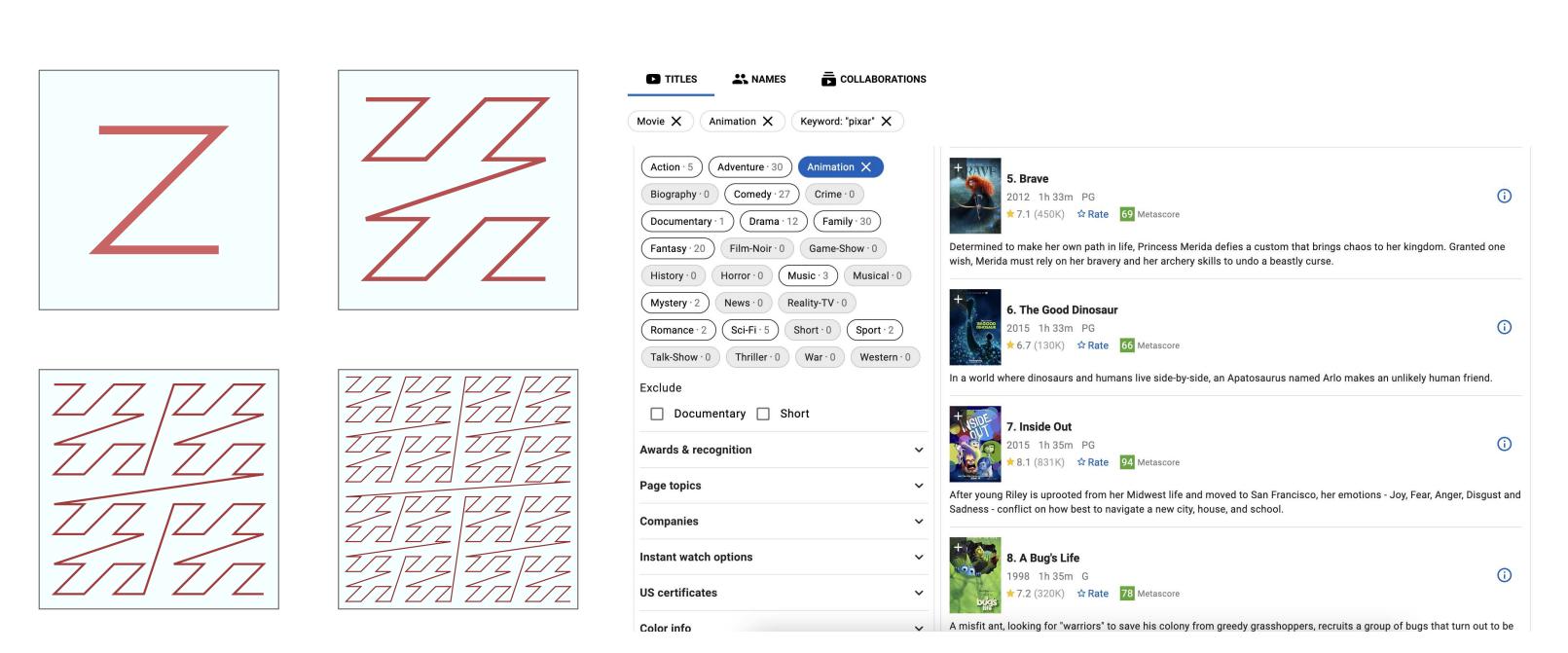
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Goals for today:

- Analyze the runtime of sorting algorithms including selection sort and insertion sort.
- Describe the steps in bucket sort and radix sort.
- Differentiate between the **best**, **worst** and **average** case runtime of an algorithm.
- Identify properties of sorting algorithms: in-place, stable.
- Customize how sorting is done for our own objects.
- Pair program to implement a sorting algorithm!



Why is sorting important?



Refresher exercise from last class: determine T(n) (an expression for the number of operations performed by the following algorithm), then provide a big-oh bound on T(n).

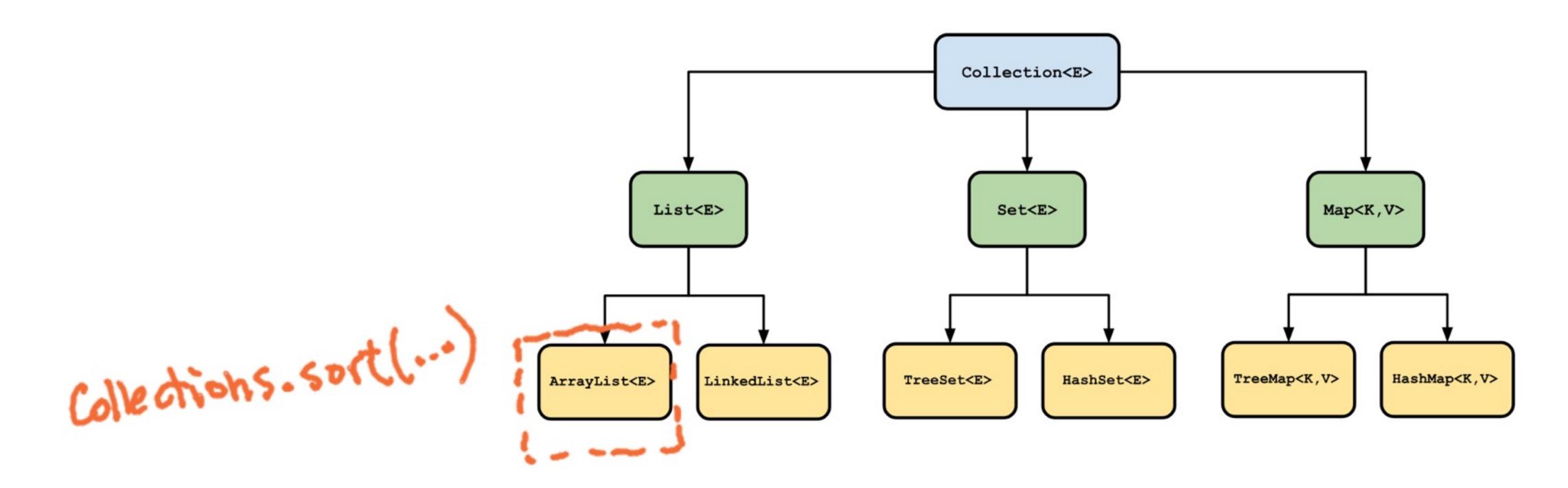
eg. " = 35

count # divisions
generalize to any n

```
int i = n;
while (i > 1) {
  i = i / 2;
}
```

```
relationship between # divisions (d)
              and n?
                    7 = n
                    d = logz(h) = T(h)
brook while loop
```

The Collections framework has built-in methods to sort.



about this

public static void sort(List<T> list)

Sorts the specified list into ascending order, according to the natural ordering of its elements. All elements in the list must implement the Comparable interface.

This sort is guaranteed to be stable: equal elements will not be 4,2,2,1 reordered as a result of the sort.

The Arrays class also has built-in static methods to sort which can be used for fixed-size arrays.

static void	sort(double[] a) Sorts the specified array into ascending numerical order.	
static void	<pre>sort(double[] a, int fromIndex, int toIndex) Sorts the specified range of the array into ascending order.</pre>	
static void	<pre>sort(float[] a) Sorts the specified array into ascending numerical order.</pre>	
static void	<pre>sort(float[] a, int fromIndex, int toIndex) Sorts the specified range of the array into ascending order.</pre>	
static void	<pre>sort(int[] a) Sorts the specified array into ascending numerical order.</pre>	
static void	<pre>sort(int[] a, int fromIndex, int toIndex) Sorts the specified range of the array into ascending order.</pre>	
static void	<pre>sort(long[] a) Sorts the specified array into ascending numerical order.</pre>	
static void	<pre>sort(long[] a, int fromIndex, int toIndex) Sorts the specified range of the array into ascending order.</pre>	
static void	<pre>sort(Object[] a) Sorts the specified array of objects into ascending order, according to the natural ordering of its elements.</pre>	
static void	<pre>sort(Object[] a, int fromIndex, int toIndex)</pre> Sorts the specified range of the specified array of objects into ascending order, according to the natural ordering of its elements.	
static void	sort(short[] a) Sorts the specified array into ascending numerical order.	10- 2-12
static void	sort(short[] a, int fromIndex, int toIndex) Sorts the specified range of the array into ascending order.	150 Tain
static <t> void</t>	<pre>sort(T[] a, Comparator< super T> c) Sorts the specimen array of bjects according to the order induced by the specified comparator.</pre>	comparator
static <t> void</t>	<pre>sort(T[] a, int fromIndex, int toIndex Comparator<? super T> c) Sorts the specified range of the specified array of objects used ling to the order induced by the specified comparator.</pre>	haday.
		4000

Arrangs, sorth...)
st.
static

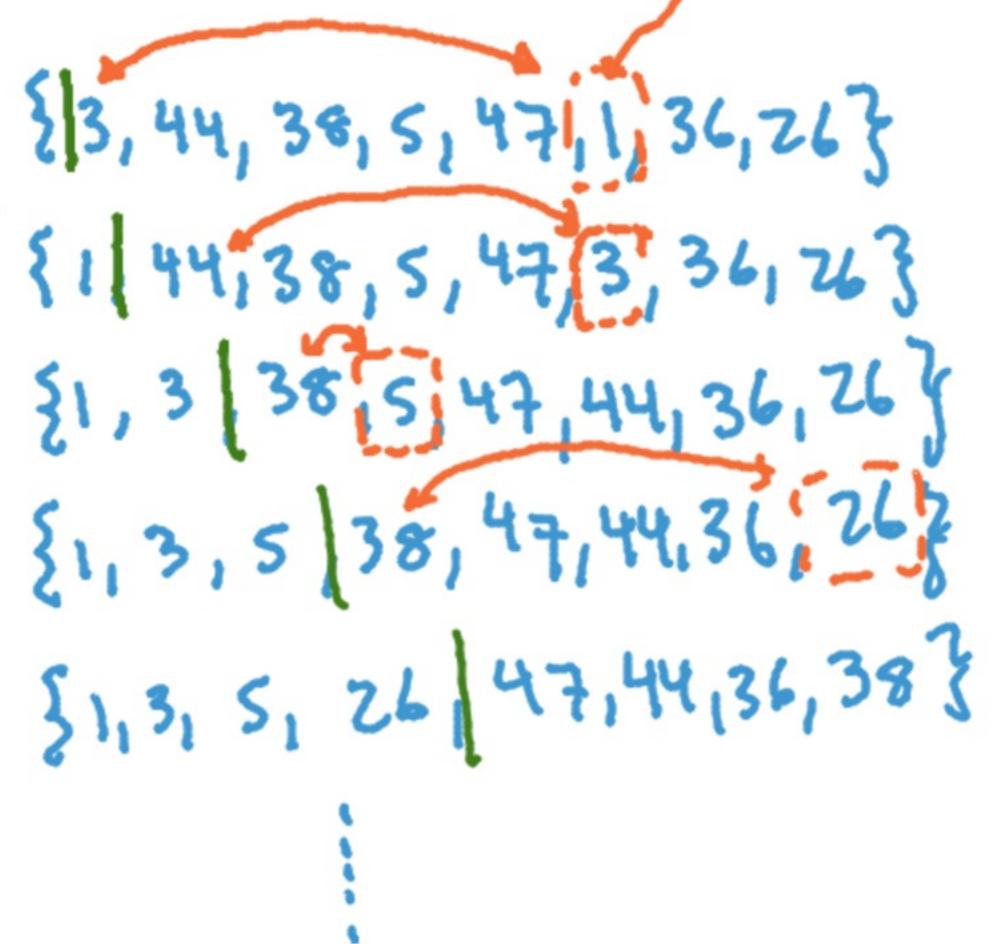
Sorting Algorithm #1 (Selection Sort):

Main idea: maintain sorted elements on the left (of some imaginary divider) and unsorted elements on the right.

- 1. Find the smallest element in unsorted part.
- 2. Swap this smallest element with the element to the right of this divider.
- 3. Move the divider to the right (by one) and go back to Step 1.

```
public static void sort(int[] items) {
  for (int i = 0; i < items.length; i++) {
    int minValue = items[i];
    int minIndex = i;
  for (int j = i + 1; j < items.length; j++) {
    if (items[j] < minValue) {
      minValue = items[j];
      minIndex = j;
    }
}

items[minIndex] = items[i];
items[i] = minValue;
}
</pre>
```

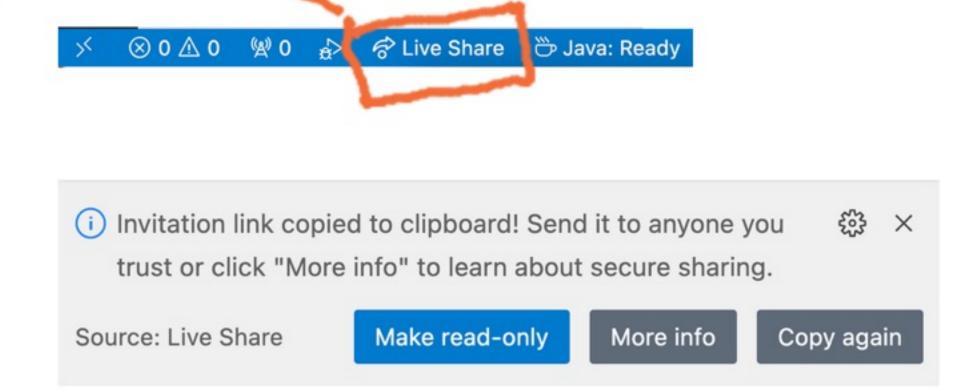


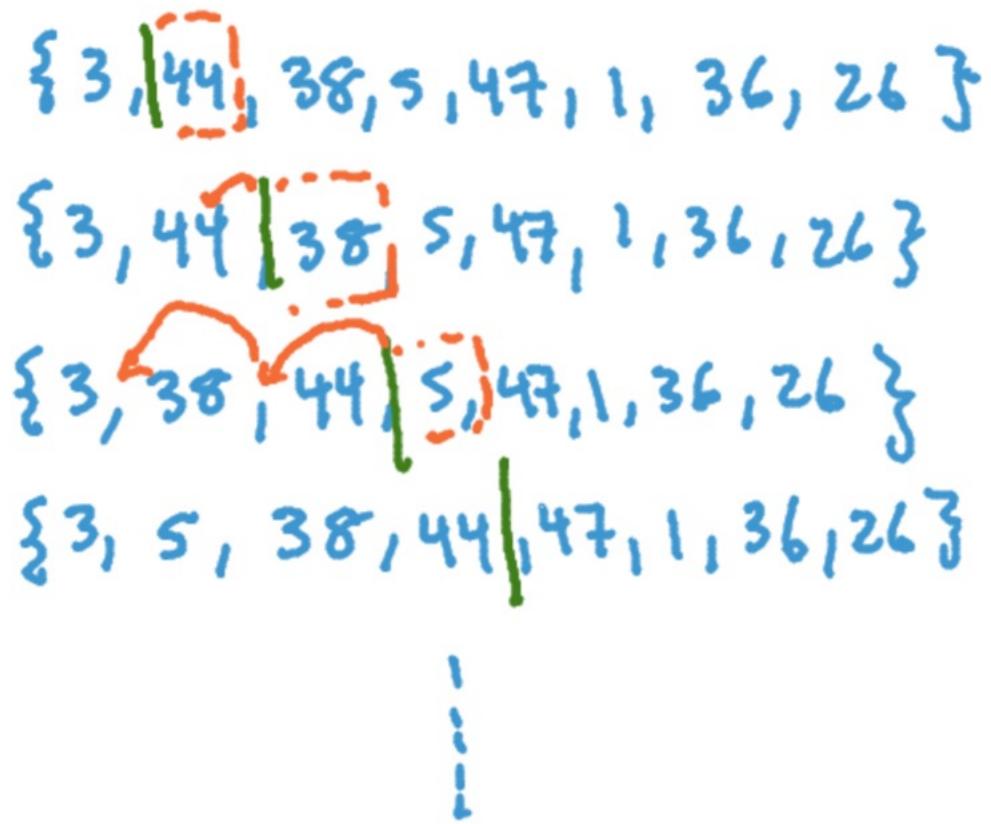
Sorting Algorithm #2 (Insertion Sort):

Main idea: maintain sorted elements on the left (of some imaginary divider) and unsorted elements on the right.

- 1. Look at first element in unsorted part (to the right of divider).
- 2. Iteratively swap this into the correct place in the sorted part.
- 3. Move the divider to the right (by one) and go back to Step 1.









Possible implementation of InsertionSort.java.

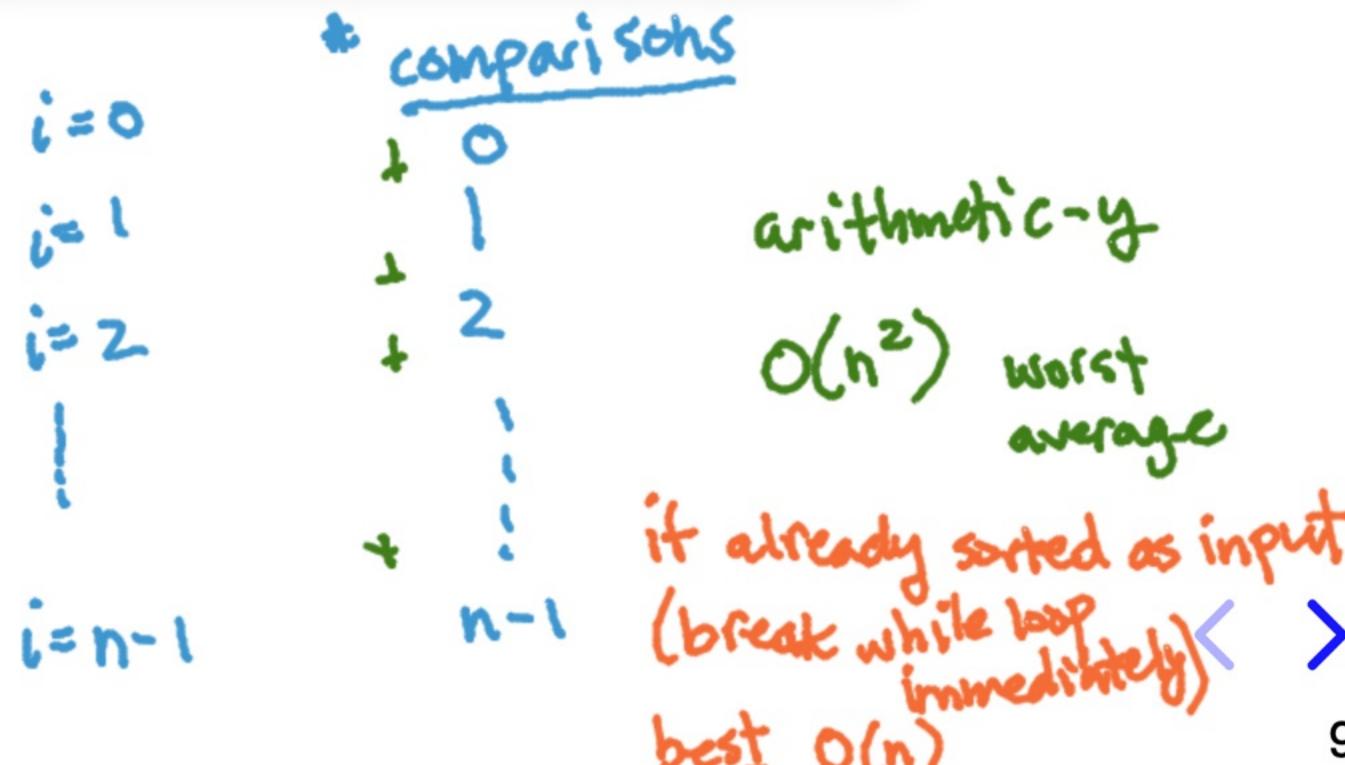
```
public static void sort(int[] items) {
    for (int i = 0; i < items.length; i++) {
        int j = i;
        while (j > 0 && items[j] < items[j - 1]) {
            // swap items at j and j - 1
            int tmp = items[j];
            items[j] = items[j - 1];
            items[j] = items[j - 1];
            items[j - 1] = tmp;
            j--;
        }
    }
}</pre>

    After implementations
    possible that
        make this more efficient.
```

Runtime analysis of selection and insertion sort.

```
// selection sort
                                                        // insertion sort
public static void sort(int[] items) {
                                                        public static void sort(int[] items) {
 for (int i = 0; i < items.length; i++) {</pre>
                                                          for (int i = 0; i < items.length; i++) {</pre>
    int minValue = items[i];
                                                            int j = i;
                                                            while (j > 0 && items[j] (< items[j - 1]) {
    int minIndex = i;
                                                              // swap items at j and y - 1
    for (int j = i + 1; j < items.length; <math>j++) {
      if (items[j]minValue) {
                                                              int tmp = items[j];
        minValue = 'tems[j];
                                                              items[j] = items[j - 1];
                                                              items[j - 1] = tmp;
        minIndex = j;
    items[minIndex] = items[i];
    items[i] = minValue;
```

```
i=0
\frac{1}{n-1}
\frac{1}{n-2}
\frac{1}{n-2}
\frac{1}{n-3}
\frac{1}{n-3}
\frac{1}{n-3}
\frac{1}{n-3}
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\frac{1}{n-1}
\frac{1}{n-2}
```



What if we want to compare our own custom objects? We have two options.

public interface Comparable<T>

need to define public int compare To (Tother Obj)

This interface imposes a total ordering on the objects of each class that implements it. This ordering is referred to as the class's natural ordering, and the class's compareTo method is referred to as its natural comparison method.

need to use keyword

public interface Comparator<T>

A comparison function, which imposes a *total ordering* on some collection of objects. Comparators can be passed to a sort method (such as Collections.sort or Arrays.sort) to allow precise control over the sort order. Comparators can also be used to control the order of certain data structures (such as sorted sets or sorted maps), or to provide an ordering for collections of objects that don't have a natural ordering.

The ordering imposed by a comparator c on a set of elements S is said to be consistent with equals if and only if c.compare(e1, e2)==0 has the same boolean value as e1.equals(e2) for every e1 and e2 in S.

what if you're using someone else's class? (and cannot modify)

nœed to define public int compare(Tobj1, Tobj2)

implementsing compareTo(Movie otherMovie) within the Movie class so it can be Comparable.

```
class Movie implements Comparable<Movie> { // make sure to import java.util.*
  public String title;
 public int year;
 public double rating;
 public Movie(String title, int year, double rating) {
   this.title = title;
   this.year = year;
   this.rating = rating;
 public int compareTo(Movie otherMovie) {
                                               defined within
   if (rating < otherMovie.rating)</pre>
     return -1;
   else if (rating > otherMovie.rating)
     return 1;
    return 0;
 public String toString() {
   return title + " (" + year + "), rating = " + rating;
```

implementsing the compare (Movie moviel, Movie movie2)
outside the Movie class to create a Comparator.

make it easier to switch

```
class MovieYearComparator implements Comparator<Movie> { // make sure to import java.util.*
 public int compare(Movie movie1, Movie movie2) {
if (movie1.year < movie2.year)</pre>
     return -1;
   else if (movie1.year > movie2.year)
     return 1;
    return 0;
class MovieTitleLengthComparator implements Comparator<Movie> {
 public int compare(Movie movie1, Movie movie2) {
    if (movie1.title.length() < movie2.title.length())</pre>
     return -1;
    else if (movie1.title.length() > movie2.title.length())
      return 1;
    return 0;
. . .
// Somewhere else in the code (possibly a PSVM) ...
// Create a Comparator<T> object and pass it to sort:
Arrays.sort(movies, new MovieYearComparator()); // sort by year
Arrays.sort(movies, new MovieTitleLengthComparator()); // sort by title length
```

between orderings

Sorting Algorithm #3 (Bucket Sort):

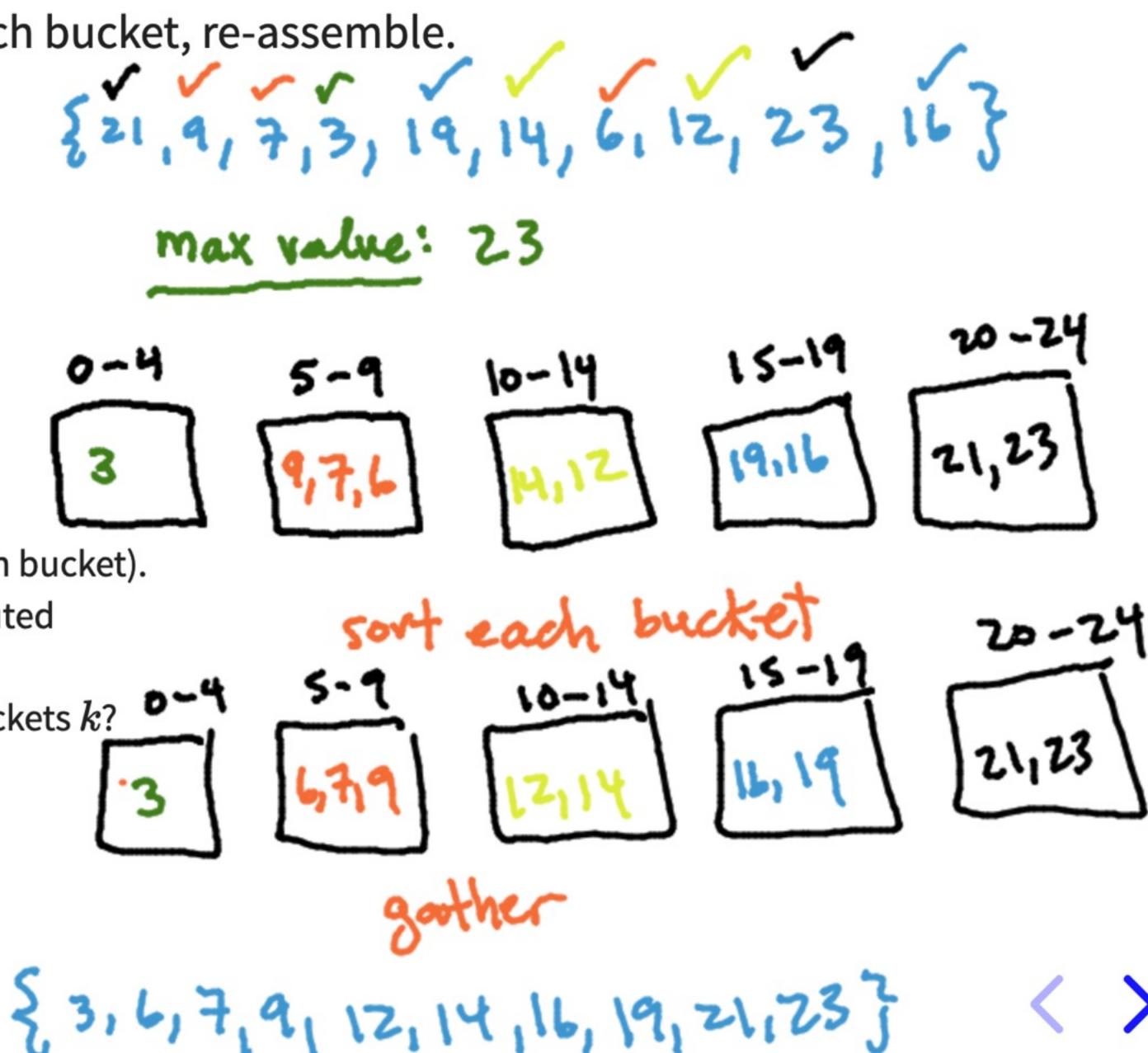
Main idea: put items in buckets, sort each bucket, re-assemble.

- 1. Set up some number of buckets k.
- 2. Scatter all n items into the appropriate bucket.
- 3. Sort each bucket.
- 4. Gather items from buckets into sorted array.

Notes:

- Does not require items to be comparable

 (unless using comparison-based sorting for each bucket).
- Works well if the input data is uniformly distributed (i.e. buckets evenly sized).
- Disadvantage: how to determine number of buckets k?
 (need information about input data).
- Worst-case runtime: $\mathcal{O}(n^2)$.
- Average-case runtime: $\mathcal{O}(n+k)$.
- Not in-place, but stable.



Sorting Algorithm #4 (Radix Sort):

max = digits = 3 = # passes = k

Main idea: similar to bucket sort, use digits to make buckets.

Ke buckets. { 170, 45, 75, 90, 2,802,2,66} { 170, 045,075, 090, 002, 802,002,066}

802

- 1. Pick a radix (base for each digit; we'll use 10).
- 2. For each digit d (starting from least significant digit):
 - 1. Make 10 empty buckets for this digit's possible values (0 9).
 - 2. Get the $d^{
 m th}$ digit of each item and put into the appropriate bucket.
 - 3. Go back through all buckets and put items from each bucket back into the original array.

Poss 2: _X 0 002, 802,002
1
2
3
7 045
S
1 20 -25
7 170,075

Notes:

- Does not require items to be comparable.
- Worst-case runtime: $\mathcal{O}(n \cdot k)$ (k is the maximum number of digits). \P
- Average-case runtime: $\mathcal{O}(n \cdot k)$.
- Not in-place, but stable.



See you tomorrow!

- We'll practice with implementing some of these sorting algorithms.
- Reminder that Noah (go/noah) and Smith (go/smith) have office hours throughout the week and the 201 Course Assistants have drop-in hours in the late afternoons/evenings (go/cshelp).
- Submit exit ticket 4R today.